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## $\boldsymbol{I} \operatorname{model} \boldsymbol{P}\left(\boldsymbol{\theta}_{\boldsymbol{i}} \mid \boldsymbol{c}_{\boldsymbol{i}}\right)=\sum \boldsymbol{P}\left(\boldsymbol{\theta}_{\boldsymbol{i}} \mid \boldsymbol{l}_{\boldsymbol{n}}, \boldsymbol{c}_{\boldsymbol{i}}\right) \boldsymbol{P}\left(\boldsymbol{l}_{\boldsymbol{n}} \mid \boldsymbol{c}_{\boldsymbol{i}}\right)$

Terminology

- $\theta_{i}=$ Points scored on possession i
- $s_{i}=$ Shooter on possession $i$
- $o_{i 1}, o_{i 2}, o_{i 3}, o_{i 4}=$ Offensive Teammates on possession $i$ - $d_{i 1}, d_{i 2}, d_{i 3}, d_{i 4}, d_{i 5}=$ Defenssive opponents on Possession $i$ - Let $c_{i}=s_{i}, o_{i 1}, o_{i 2}, o_{i 3}, o_{i 4}, d_{i 1}, d_{i 2}, d_{i 3}, d_{i 4}, d_{i 5}$ Want to model $P\left(\theta_{i} \mid c_{i}\right)$
- Divide court into n locations, $l_{1, \ldots}, l_{n}$

Can also add position dummies for players on court - \{Guard, Forward, Center\}

Caveat: do not model fouls at all


## Estimate:

- Player's \{tendency to shoot, ability to score\} from court locations
- Player's influence on teammates' \{tendency to shoot, ability to score\} from court locations
- Player's influence on opponents' \{tendency to shoot, ability to score\} from court locations
- Position averages for all the above (See visualizations to right)


## Novel Features

Shooting ( $s_{i}$ )
Allows for independent estimates of a players tendency to shoot from a location \& their ability to score from there More granular court locations than usual Inclusion of position dummies, and estimation of their coefficients

## Metrics

Parameters
Season: 2017-18
Train set is first 1100 games
(189K shots)
Test set is last 130 games (23K shots)

For the purposes of equal comparison, all models are compared using multiclass log loss.
The classes which the loss is calculated on are the most abstract outcomes of a shot

Zero points scored
Two points scored

- Three points scored

When the modeling more granular outcomes than just these three, those are aggregated up to these three classes

Future Work
Utilize $x, y$ coordinates of shot Combine location tendencies/shooting ability into one visualization
Model who will shoo
Combine in larger graphical mode

| Model Features | Model Target/s | $\begin{array}{\|l\|} \hline \text { 0-PT } \\ \text { loggoss } \end{array}$ | $\begin{aligned} & \text { 2-PT } \\ & \text { logloss } \end{aligned}$ | $\begin{aligned} & \text { 3-PT } \\ & \text { logloss } \end{aligned}$ | AVG logloss |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Miss |  |  |  |  |
| None (Baseline) | Made 2 pointer |  |  |  |  |
| For estimate use train set means | Made 3 pointer | 0.6896 | 0.6393 | 0.3683 | 0.5657 |

Conditional on knowing the shooter:

| Model Features | Model Target/s | $\begin{array}{\|l\|} \hline \text { 0-PT } \\ \text { logloss } \end{array}$ | $\begin{array}{\|l\|} \hline \text { 2-PT } \\ \text { logloss } \end{array}$ | $\begin{array}{\|l\|} \hline \text { 3-PT } \\ \text { logloss } \end{array}$ | AVG logloss |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Shooter dummy | Location (multinomial, $\mathrm{n}=7$ ) |  |  |  |  |
| Offensive teammate dummies | For each location fit |  |  |  |  |
| Defensive opponents dummies | separate make/miss |  |  |  |  |
| Positional dummies | classifier | 0.6856 | 0.6144 | 0.3427 | 0.5475 |
| Shooter dummy |  |  |  |  |  |
| Offensive teammate dummies |  |  |  |  |  |
| Defensive opponents dummies | Multinomial - Miss, |  |  |  |  |
| Positional dummies | Made 2pt, Made 3pt | 0.6931 | 0.6201 | 0.3489 | 0.554 |
|  | Location (multinomial, $\mathrm{n}=7$ ) |  |  |  |  |
| Shooter dummy | For each location fit |  |  |  |  |
| Offensive teammate dummies | separate make/miss |  |  |  |  |
| Defensive opponents dummies | classifier | 0.6859 | 0.6155 | 0.3435 | 0.5483 |



Not conditional on knowing the shooter

| Model Features | Model Target/s | $\begin{array}{l\|} \hline \text { 0-PT } \\ \text { logloss } \end{array}$ | $\begin{array}{\|l\|} \hline \text { 2-PT } \\ \text { logloss } \end{array}$ | $\begin{array}{\|l\|} \hline \text { 3-PT } \\ \text { logloss } \end{array}$ | AVG logloss |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Shooter dummy, offensive teammate dummies, defensive opponents dummies, positional dummies | Location (multinomial, $n=7$ ), for each location fit separate make/miss classifier | 0.6893 | 0.6386 | 0.367 | 0.565 |
| Offensive player dummies, defensive opponents dummies, positional dummies | Multinomial - Miss, Made 2pt, Made 3pt | 0.692 | 0.6395 | 0.3682 | 0.5666 |



Which players would LeBron help score the most efficiently (controlling for position)


